Spatial Crossover Between Far-From-Equilibrium and Near-Equilibrium Dynamics in Locally Driven Suspensions

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We examine the response of a quasi-two-dimensional colloidal suspension to a localized circular driving induced by optical tweezers. This approach allows us to resolve over 3 orders of magnitude in the Péclet number (Pe) and provide a direct observation of a sharp spatial crossover from far- to near-thermal-equilibrium regions of the suspension. In particular, particles migrate from high to low Pe regions and form strongly inhomogeneous steady-state density profiles with an emerging length scale that does not depend on the particle density and is set by Pe \approx 1. We show that the phenomenological two phase fluid constitutive model is in line with our results.

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Complex fluids comprise a family of fluids which include elements of intermediate size; elements which are larger compared to the molecules forming the embedding liquid and smaller compared to a typical macroscopic length scale. Among many (e.g., solutions of long polymer chains), suspensions of hard spheres, which we address here, are probably the simplest example.

Over the years extensive efforts have been invested in exploring the flow behavior of hard sphere suspensions at conditions that are far-from-thermal equilibrium (i.e., non-Brownian suspension) [1,2] both experimentally and by modeling. Strong driving significantly modifies the microstructure of the immersed particles [3-5]. The coupling between microstructure and hydrodynamic interactions between particles [3,6], and the frictional contact between the particles [7,8], result in a rich phenomenology which is dramatically different from that of Newtonian fluids. This includes a strong rate dependence of viscosity and the emergence of normal stresses [2,9]. The latter, in particular, does not have any equivalence in classical fluids and gives rise to large scale motion (migration) of particles relative to the embedding liquid [1,2,10–13]. Resulting large scale variations in the particle density, in turn, affect the overall flow of the composite fluid.

In contrast to the far-from-thermal-equilibrium limit, where the Brownian motion of the particles has negligible contribution, migration at the near-equilibrium regime requires understanding of the interplay between particle flow and their thermal fluctuations. Although the former has been extensively explored in experiments, the study of the latter largely relies on numerical simulations. Here we provide measurements of particle migration at both high and low strain rate regimes and directly resolve the spatial crossover between the two. We characterize this crossover across a wide range of driving rates and particle densities, and show that a previously suggested phenomenological two phase fluid constitutive model [14] is in line with our observations.

To this end, we adopt a bottom-up approach. We probe the response of a colloidal suspension to local driving on a single particle level [15–22]. This is in contrast to traditional methods such as rheology, that focus on the flow behavior caused by imposing bulk forces on macroscopic samples [2].

Our experimental system is schematically presented in Fig. 1(a). We let two types of spherical colloidal particles sediment and form a quasi-two-dimensional (2D) layer in a range of area fractions $0.1 < \phi_0 < 0.4$. For the majority phase, bath particles, we use 3-trimethoxysilyl propyl methacrylate (TPM) [23] with a radius of $a = 1.35 \pm 0.05 \,\mu\text{m}$ [24]. A Melamine-formaldehyde (MF) particle ($a = 1 \pm 0.03 \,\mu\text{m}$, Sigma-Aldrich) is trapped above the glass plate and prescribed a circular trajectory by using optical tweezers. Linear driving frequencies are varied within a range of 0.1 < f < 10 Hz. Any inertia effects, including centrifugal forces, are negligible due to the low Reynolds numbers Re $< 10^{-6}$ conditions. Self-diffusion of the sedimented bath particles near the bottom solid plane [25,26] is measured to be $D \approx 0.05 \,\mu\text{m}^2$ /sec.

An inverted microscope (Olympus IX71) with a $60 \times$ objective (Olympus, oil immersion, NA = 1.42) is used to image the particles and focus the trapping laser beam ($\lambda = 1083$ nm). A circular motion of the trapped particle is prescribed by deflecting the laser beam with a piezo tip-tilt platform (Physik Instrumente (PI) GmbH & Co. KG) [18,27]. Particles are dispersed in an organic solvent mixture of 40/60 (by volume) Tetralin and Decalin, and commercial dispersant OLOA 1200 (~1% by weight).



FIG. 1. Steady-state flow and density profiles of a locally driven colloidal suspension. (a) A 2D layer of TPM particles is formed by sedimentation in a sealed cell with thickness w $\approx 170 \ \mu m$. A MF particle is trapped at $h \approx 2 \ \mu m$ above the coverslip by a focused IR laser beam and prescribed a circular trajectory with a radius $R = 3.35 \ \mu m$ (green line). (b) Index of refraction of the solvent and the bath particles (TPM) were chosen to match closely (inset) so that interactions between the laser and TPM particles are negligible. Once the image contrast is enhanced, particle trajectories can be tracked. Five selected trajectories of the bath particles over a period of 20 s are superimposed. (c) Particle velocity field V reveals azimuthal flow spanning 3 orders of magnitude within the field of view. Note the logarithmic color axis. (d) Measured local area fraction $\phi(x, y)$ show a highly nonhomogeneous steady-state profile formed by particles migrating from high to low strain rate regions. Here $\phi(x, y) = n(x, y) \cdot \pi a^2$, where n(x, y) is the local number density. (b)-(d) The prescribed driving frequency and equilibrium area fraction are f = 10 Hz and $\phi_0 = 0.3$, respectively. Spatial profiles of V and ϕ where obtained by temporal averaging of the measurements over a period of ~40 min and further smoothed spatially over $0.5 \times 0.5 \ \mu m^2$ regions. The trapped particle is excluded in the V and ϕ color plots.

The index of refraction, n, of the solvent, nearly matches the index of refraction of the TPM particles [Fig. 1(b), inset]. Since optical trapping depends on the refractive index mismatch between particle and medium, we can manipulate the MF ($n \approx 1.68$) particles while barely affecting the TPM particles ($n \approx 1.5$) with the laser light. The positions of the TPM particles can be located and tracked [28] by processing the images [Fig. 1(b)] as a result of a small remaining mismatch in n. Further details appear in the Supplemental Material [29].

A typical example of a steady-state response of the suspension to a local rotational driving is presented in Fig. 1. Figure 1(b) demonstrates particle trajectories over a fraction of the experiment duration (see also the movie in [29]). The prescribed circular trajectory of the driven particle induces an average rotational flow profile of the

bath particles with velocity amplitudes that span 3 orders of magnitude within our field of view [Fig. 1(c)]. Figure 1(d) shows the resulting highly nonuniform spatial profile of the particle density (presented in terms of an area fraction ϕ) that is formed by migration of particles from high to low flow rate regions. This rearrangement of the particles, in the absence of an external potential, is a first confirmation of the strong out-of-equilibrium conditions. Nevertheless, it is evident that the formed depletion region is localized to the vicinity of the driving and the suspension recovers equilibrium conditions at $r \gg R$. The measured $\phi(r)$ profile, therefore, provides a direct observation of the spatial crossover between the out-of-equilibrium and the unaffected equilibrium regions. In what follows we characterize particle flow, particle migration, and the crossover to equilibrium, and compare our measurements with a twophase constitutive model for colloidal suspensions.

We start by quantifying and modeling the induced rotational flow of the particles. Figure 2(a) demonstrates that the averaged azimuthal particle velocity profiles $V_{\theta}(r)$ are roughly independent of ϕ_0 . Similarly, measurements of the particle-particle hydrodynamic interactions [Fig. 2(b)] and short time self-diffusion [26] show only slight dependence on ϕ_0 for $\phi_0 < 0.4$ [29]. We neglect, therefore, interactions between the bath particles and model the flow field through hydrodynamic pair interactions between the driven and bath particles that appear in an incompressible viscous liquid at vanishing Reynolds number. The form of the hydrodynamic interactions depends on the spatial confinement of the fluid [32]. Here, we consider particle motion at height h above a solid plane. The velocity of particle 2, as a result of a motion of particle 1, is given by $v_i^2 = \tilde{B}_{ij}^{12}(\vec{r}_{12}; h, a^1)v_j^1$, where \tilde{B}_{ij}^{12} is proportional to the mobility tensor ([29] and [33]). The eigenvalues of \tilde{B}_{ij}^{12} , within the leading order in h/r, are $\tilde{B}_{\parallel}^{12} \sim 1/r^3$ and $\tilde{B}_{\perp}^{12} \sim 1/r^5$, where \parallel and \perp symbols denote parallel and perpendicular directions relative to \vec{r}_{12} , respectively. Once a circular path of particle 1 is prescribed, the trajectory of particle 2 is readily integrated. Such periodic driving results in a "sawtooth" motion [Fig. 2(b)] and is consistent with our measured trajectories [Fig. 1(b)]. We obtain an analytical expression for the average particle rotational velocity [29] which decays as $V_{\theta} \sim 1/r^4$.

These predictions for V_{θ} and $\tilde{B}_{\parallel}^{12}$ describe our measurements asymptotically $(r \gg R)$, as shown by the dashed black lines in Figs. 2(a) and 2(b), respectively. A solution for \tilde{B}_{ij}^{12} for all orders in h/r [34], and the corresponding integration of V_{θ} [29], provide an excellent description of our measurements at all distances with no adjustable parameters [solid black lines in Figs. 2(a) and 2(b)]. We conclude therefore that the average particle flow can be well approximated by the hydrodynamic pair interactions near a solid plane.

The balance between the shear rate $\dot{\gamma}$ and the Brownian relaxation time a^2/D is characterized by the Péclet number



FIG. 2. Induced particle flow by a local rotational driving. (a) Average azimuthal particle velocity V_{θ} at two driving frequencies. Solid lines at the top-left corner denote the velocity and size of the driven particle. [(b), illustration] Green and blue are the driven and bath particles, respectively. Separation vector is denoted by \vec{r}_{12} . The trajectory of the bath particles (purple) is calculated by integrating the flow field resulting from the prescribed circular motion of the driven particle. Compare the sawtooth trajectories with the measurements presented in Fig. 1(b). [(b), main figure] Averaged ratio of v_{\parallel}^1 and v_{\parallel}^2 , parallel velocity components with respect to \vec{r}_{12} , provides a measure of the parallel eigenvalue of the mobility tensor $\tilde{B}_{ii}^{12}(\vec{r}_{12})$ (see main text and [29] for details). Both f = 1 and f = 10 Hz datasets are included. (a),(b) Colors denote experiments with different equilibrium area fractions ϕ_0 . The asymptotic solution $(|\vec{r}_{12}| \gg h \text{ and }$ $r \gg h$ [33] and corrected result [34] are denoted by dashed and solid lines, respectively.

Pe = $|\dot{r}|a^2/D$. Measured $V_{\theta}(r)$ profiles together with $\dot{\gamma}_{\theta r} = r\partial_r(V_{\theta}/r)$, the only nonvanishing component of the strain-rate tensor in case of a 2D rotational flow [35], reveal therefore that Pe $(r) \sim 1/r^5$. An important characteristic of our setup is the ability to spatially resolve a wide range of Pe [0.1 < Pe(r) < 100] and access the near and far-from-equilibrium regimes in a single experiment.

In Fig. 3 we address the evolved microstructure of our colloidal suspension at both high and low Pe regions by characterizing the 2D pair correlation function $g(x_1, x_2)$. In order to account for the spatial variations in Pe we calculate $g(x_1, x_2)$ only with respect to the particles that are included in a narrow ring at a distance of interest *r* from the center of the rotational flow [see Fig. 3(a) for details]. Here x_1 and x_2 denote the spatial coordinates in the parallel $\hat{\theta}$ and perpendicular \hat{r} directions with respect to the flow. The rotational symmetry and the steady-state conditions of the flow allow us to average $g(x_1, x_2)$ over both the particles within the ring and time. The $g(x_1, x_2)$ maps obtained far and near the driving, corresponding to low and high Pe regions, are presented in Figs. 3(b) and 3(c), respectively.

At low Pe regions, where particle diffusion dominates particle advection, $g(x_1, x_2)$ show an isotropic form [Fig. 3(b)] that indicates an equal probability of finding a particle at any direction with respect to any other particle. At higher Pe values, however, this symmetry is highly distorted [Fig. 3(c)] [4,5,37,38]. This broken symmetry of $g(x_1, x_2)$ reflects the direction of shear—the probability of observing two particles in close vicinity is significantly increased in the second and fourth quadrants (compression)



FIG. 3. Pair correlation function near- and far-from-thermal equilibrium. (a) For any snapshot in time, as radial gradients in Pe(r) are present, $g(x_1, x_2)$ is calculated for particles in a narrow ring (0.1 μ m thick) at distance r from the center (orange particles). Statistics are enhanced by averaging over time and the particles within the ring by using a polar coordinate system $(\hat{r}, \hat{\theta})$. Here x_1 and x_2 denote local spatial coordinates in the directions of $\hat{\theta}$ and \hat{r} , respectively. Measured $g(x_1, x_2)$ far from (b) and near (c) the driving region demonstrate the symmetry breaking at far-from equilibrium conditions. $\phi_0 = 0.3$, f = 10 Hz, corresponding to the experiment presented in Fig. 1. (d) At equilibrium (no driving), osmotic pressure (blue dots) is inferred from measurements of q (see main text and [29]). The uncertainty is roughly represented by the size of the symbols. Theoretical predictions for 2D layer of hard spheres [36] is denoted by the black solid line (see main text for more details).

and depleted in the tension quadrants. The modified microstructure (local rearrangement) of the immersed particles is a clear signature of nonequilibrium dynamics and a key ingredient in the emergence of nonlinear stresses [3]. These stresses, in turn, drive the observed spatial variations in $\phi(r)$ on larger length scales [Fig. 1(d)].

We now characterize the steady state spatial $\phi(r)$ profiles and the crossover to equilibrium. Figure 4(a), left, presents the measured $\phi(r)$ profiles for a wide range of driving rates. Evidently, increasing driving rates amplify particle migration, which in turn results in stronger gradients in $\phi(r)$ and wider particle depletion regions. All profiles of $\phi(r)$ collapse to a single functional form [Fig. 4(a), right] when r is rescaled by the distance where shear and Brownian motions are comparable $r(\text{Pe} = 1) \sim (v^1)^{1/5}$. This emerging length scale that characterizes the spatial crossover from far- to near-equilibrium conditions of the suspension is a direct result of the interplay between the flow and thermal fluctuations and is not present in traditional large scale rheometry experiments of non-Brownian suspensions, where particle migration is only limited by the system size [13]. In Fig. 4(b) we further compare a series



FIG. 4. Comparing measured density profiles with the rheological constitutive model. (a) Measured radial density profiles, $\phi(r)$ for increasing driving rate. (right) $\phi(r)$ profiles collapse to a single functional form when plotted with respect to r/r(Pe = 1), where r(Pe = 1) denotes the radial distance where shearing motion and particle diffusion are comparable. (b) $\phi(r)$ for increasing equilibrium density ϕ_0 . All density profiles collapse when scaled by equilibrium values ϕ_0 . Uncertainties in local ϕ values are ± 0.01 for $\phi_0 = 0.13$, 0.2 and ± 0.02 for $\phi_0 = 0.3$, 0.4 [29]. (a),(b) Solid lines denote predictions of the constitutive model [Eq. (1)] for $\lambda_{rr} = \lambda_{\theta\theta} = 2$.

of experiments with various equilibrium particle area fractions ϕ_0 . Within the explored range $0.1 < \phi_0 < 0.4$, all profiles of ϕ scale with ϕ_0 [Fig. 4(b), right]. This observation demonstrates that the crossover between low and high Pe limits does not depend on the particle density.

To account for these observations we turn to the phenomenological two-phase fluid model [12], where motion of the particles relative to the embedding liquid is considered. In this model, particle contributions to the bulk normal stresses drive radial particle flux $\mathbf{j} \sim -\nabla \cdot \Sigma^p$. However, since direct measurements of $\Sigma_{ii}^p(\phi, \text{Pe})$ are challenging [39] and the exact form across a wide range of ϕ and Pe values is subject to debate [2,13,40,41], the total flux is assumed to be the sum of two asymptotic behaviors [14]. Namely, shear driven (Pe \gg 1) and osmotic pressure driven (Pe \ll 1) \mathbf{j}_j and \mathbf{j}_B , respectively.

In the presence of strong shearing motion (Pe \gg 1) the dominant hydrodynamic interactions and asymmetric pair correlation function [Fig. 3(c)] give rise to normal stresses $\Sigma_{ii}^{\dot{\gamma}} \sim |\dot{\gamma}|$. Gradients in $\dot{\gamma}$ result in particle flux $\mathbf{j}_{\dot{\gamma}} \sim -\nabla \cdot \mathbf{\Sigma}^{\dot{\gamma}}$, a process often referred to as shear induced particle migration [2,12]. Here, we limit the complexity of the constitutive model, and use a simplified stress form predicted for dilute 3D suspensions $\Sigma_{ii}^{\dot{\gamma}} = \lambda_{ii}\eta |\dot{\gamma}|\phi^2$ [3,12–14], where λ_{rr} and $\lambda_{\theta\theta}$ signify the normal stress anisotropy. We adapt this 3D stress form to the quasi-2D nature of our system by assuming that the thickness of the

colloidal layer scales with the particle radius *a*, and use $\Sigma_{ii}^{\dot{\gamma}} = a\lambda_{ii}\eta|\dot{\gamma}|\phi^2$.

At vanishing Pe values, Brownian motion of the particles results in osmotic pressure $\Pi(\phi)$. Any gradients in the particle density will result in a flux of particles $\mathbf{j}_B \sim -\nabla \Pi$. In case of a 2D layer of hard spheres, osmotic pressure is related to $g(\vec{r}_{12})$ through $\Pi \pi a^2/kT = \phi[1 + 2\phi g(2a; \phi)]$, where g(2a) denotes the pair correlation value at particle contact [36]. Measurements of g(2a), therefore, allow us to infer $\Pi(\phi)$ of the suspension [42,43]. Here we neglect the slight repulsion between the particles, and map our system to the hard sphere case by approximating g(2a) with the maximal $g(\vec{r}_{12})$ value [29]. Figure 3(d) demonstrates that, for colloidal suspensions at equilibrium (no driving), the obtained values of $\Pi(\phi)$ agree well with the theoretical predictions $\Pi \pi a^2/kT = \phi/(1 - \phi)^2$ [36] and are consistent with previous experimental observations [44].

Finally, we model the crossover between the high and low Pe regimes and the resulting steady-state spatial profiles $\phi(r)$ (Fig. 4) by balancing the two origins of the radial particle flux $\mathbf{j}_B + \mathbf{j}_{\dot{r}} = 0$. In case of a 2D rotational flow, therefore, $\phi(r)$ are obtained by solving

$$0 = \partial_r \left[\frac{\phi}{(1-\phi)^2} + \frac{1}{6} \lambda_{rr} \operatorname{Pe} \phi^2 \right] - \frac{1}{6} (\lambda_{\theta\theta} - \lambda_{rr}) \frac{\operatorname{Pe} \phi^2}{r} \qquad (1)$$

with the boundary conditions $\phi(r \to \infty) = \phi_0$. Here, Pe(*r*) profiles are inferred from the measured particle velocities [Fig. 2(a)], whereas λ_{rr} and $\lambda_{\theta\theta}$ remain to be determined.

Solutions to Eq. (1) describe our measurements well in a broad range of driving rates [Fig. 4(a)] and particle concentrations [Fig. 4(b)] for $\lambda_{rr} = \lambda_{\theta\theta} = 2$. Specifically, the model captures successfully the spatial crossover between the high Pe regime and equilibrium. Any deviations of the model from the scaling in ϕ_0 , as a result of the nonlinearity of Eq. (1), are beyond the resolution of our measurements.

We note that the particular choice of $\lambda_{ii} = 2$ is motivated by an attempt to maintain simplicity of the model, whereas a strict constraint on λ_{ii} proves to be difficult; a similar level of agreement between the model and measurements can be obtained in a range between $\lambda_{rr} \approx 3$, $\lambda_{\theta\theta} \approx 1$ and $\lambda_{rr} \approx 1$, $\lambda_{\theta\theta} \approx 3$. These values are consistent with other studies in various 3D geometries [12,14,22], which show that λ_{rr} and $\lambda_{\theta\theta}$ are typically of order unity.

While the constitutive model captures the average spatial form of the density profiles, it fails to describe their detailed structure. Particle excluded volume gives rise to strong oscillations in $\phi(r)$ (Fig. 4), which suggests the formation of a layered structure. These particle correlations are increasing with the particle density, but also smeared out by an increasing shear rate. As the model we consider here essentially provides a continuum description of the fluid, density correlations on the particle scale are beyond its range of applicability. In fact, it is compelling that a

continuum model provides such a good description on length scales that are comparable to the particle size.

One unique feature of our system is that the response of the environment (bath particles) occurs on time scales comparable to the driving rate. This is in striking contrast to traditional colloidal model systems studied in the context of stochastic thermodynamics out of equilibrium [45–47]. We suggest, therefore, that our mean-field continuum analysis provides a starting point to explore various out-of-equilibrium statistical mechanics observables such as self- and pair-diffusion, entropy production, and fluctuations in driven systems where bath dynamics cannot be neglected.

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- M. M. Denn and J. F. Morris, Annu. Rev. Chem. Biomol. Eng. 5, 203 (2014).
- [2] I. Guazzelli and O. Pouliquen, J. Fluid Mech. 852, P1 (2018).
- [3] J. F. Brady and J. F. Morris, J. Fluid Mech. 348, 103 (1997).
- [4] X. Cheng, J. H. McCoy, J. N. Israelachvili, and I. Cohen, Science 333, 1276 (2011).
- [5] F. Blanc, E. Lemaire, A. Meunier, and F. Peters, J. Rheol. 57, 273 (2013).
- [6] D. R. Foss and J. F. Brady, J. Fluid Mech. 407, 167 (2000).
- [7] N. Y. C. Lin, B. M. Guy, M. Hermes, C. Ness, J. Sun, W. C. K. Poon, and I. Cohen, Phys. Rev. Lett. 115, 228304 (2015).
- [8] R. Mari, R. Seto, J. F. Morris, and M. M. Denn, Proc. Natl. Acad. Sci. U.S.A. 112, 15326 (2015).
- [9] E. Brown and H. M. Jaeger, Rep. Prog. Phys. 77, 046602 (2014).
- [10] F. GadalaMaria and A. Acrivos, J. Rheol. 24, 799 (1980).
- [11] D. Leighton and A. Acrivos, J. Fluid Mech. 181, 415 (1987).
- [12] J. F. Morris and F. Boulay, J. Rheol. 43, 1213 (1999).
- [13] F. Boyer, O. Pouliquen, and I. Guazzelli, J. Fluid Mech. 686, 5 (2011).
- [14] M. Frank, D. Anderson, E. R. Weeks, and J. F. Morris, J. Fluid Mech. 493, 363 (2003).
- [15] P. Habdas, D. Schaar, A. C. Levitt, and E. R. Weeks, Europhys. Lett. 67, 477 (2004).
- [16] R. P. A. Dullens and C. Bechinger, Phys. Rev. Lett. 107, 138301 (2011).
- [17] J. Pesic, J. Z. Terdik, X. Xu, Y. Tian, A. Lopez, S. A. Rice, A. R. Dinner, and N. F. Scherer, Phys. Rev. E 86, 031403 (2012).
- [18] J. R. Gomez-Solano and C. Bechinger, Europhys. Lett. 108, 54008 (2014).
- [19] I. Buttinoni, Z. A. Zell, T. M. Squires, and L. Isa, Soft Matter 11, 8313 (2015).

- [20] I. Buttinoni, M. Steinacher, H. T. Spanke, J. Pokki, S. Bahmann, B. Nelson, G. Foffi, and L. Isa, Phys. Rev. E 95, 012610 (2017).
- [21] A. Ortiz-Ambriz, S. Gerloff, S. H. L. Klapp, J. Ortn, and P. Tierno, Soft Matter 14, 5121 (2018).
- [22] R. N. Zia, Annu. Rev. Fluid Mech. 50, 371 (2018).
- [23] Y. Liu, K. V. Edmond, A. Curran, C. Bryant, B. Peng, D. G. A. L. Aarts, S. Sacanna, and R. P. A. Dullens, Adv. Mater. 28, 8001 (2016).
- [24] Courtesy of Prof. Roel Dullens from the Department of Chemistry, Oxford, GB.
- [25] A. Sonn-Segev, J. Bawzdziewicz, E. Wajnryb, M. L. Ekiel-Jeewska, H. Diamant, and Y. Roichman, J. Chem. Phys. 143, 074704 (2015).
- [26] A. L. Thorneywork, R. E. Rozas, R. P. A. Dullens, and J. Horbach, Phys. Rev. Lett. **115**, 268301 (2015).
- [27] L. P. Faucheux, G. Stolovitzky, and A. Libchaber, Phys. Rev. E 51, 5239 (1995).
- [28] J. C. Crocker and D. G. Grier, J. Colloid Interface Sci. 179, 298 (1996).
- [29] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.127.038003 for detailed experimental method description and the calculation of the hydrodynamic interactions near a planar surface, which includes Refs. [30,31].
- [30] C. Middleton, M. D. Hannel, A. D. Hollingsworth, D. J. Pine, and D. G. Grier, Langmuir 35, 6602 (2019).
- [31] J. A. Anderson, J. Glaser, and S. C. Glotzer, Comput. Mater. Sci. 173, 109363 (2020).
- [32] H. Diamant, J. Phys. Soc. Jpn. 78, 041002 (2009).
- [33] J. Happel and H. Brenner, Low Reynolds Number Hydrodynamics (Springer, Netherlands, 1983).
- [34] E. R. Dufresne, T. M. Squires, M. P. Brenner, and D. G. Grier, Phys. Rev. Lett. 85, 3317 (2000).
- [35] L. D. Landau and E. M. Lifshitz, *Fluid Mechanics* (Pergamon Press, New York, 1987).
- [36] E. Helfand, H. L. Frisch, and J. L. Lebowitz, J. Chem. Phys. 34, 1037 (1961).
- [37] N. Y. C. Lin, S. Goyal, X. Cheng, R. N. Zia, F. A. Escobedo, and I. Cohen, Phys. Rev. E 88, 062309 (2013).
- [38] C. Gao, S. D. Kulkarni, J. F. Morris, and J. F. Gilchrist, Phys. Rev. E 81, 041403 (2010).
- [39] T. Dbouk, L. Lobry, and E. Lemaire, J. Fluid Mech. 715, 239 (2013).
- [40] H. C. W. Chu and R. N. Zia, J. Rheol. 60, 755 (2016).
- [41] R. Seto and G.G. Giusteri, J. Fluid Mech. 857, 200 (2018).
- [42] J. F. Brady, J. Chem. Phys. 99, 567 (1993).
- [43] N. Y. C. Lin, M. Bierbaum, P. Schall, J. P. Sethna, and I. Cohen, Nat. Mater. 15, 1172 (2016).
- [44] A. L. Thorneywork, J. L. Abbott, D. G. A. L. Aarts, and R. P. A. Dullens, Phys. Rev. Lett. 118, 158001 (2017).
- [45] U. Seifert, Rep. Prog. Phys. 75, 126001 (2012).
- [46] V. Blickle, T. Speck, L. Helden, U. Seifert, and C. Bechinger, Phys. Rev. Lett. 96, 070603 (2006).
- [47] A. Bérut, A. Petrosyan, and S. Ciliberto, Europhys. Lett. 107, 60004 (2014).